

# Semianalytical Universal Simulation of the Electrical Properties of the Permeable Base Transistor

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## Abstract

Using only a few numerical calculations, we give the analytical current-voltage and charge-voltage characteristics valid for any PBT. The highest unity current gain frequency ( $f_r$ ) corresponding to the current technology is on the order of 30 GHz ; nevertheless, the oscillation frequency can be higher than 100 GHz.

## 1. Introduction

There are two types of PBT : the buried base PBT, and the etched groove PBT [1].

The PBT is essentially a two dimensional structure ; it is so impossible to find *ab initio* analytical expressions for its characteristics. The optimization of the device needs time consuming 2-D programs, and in particular, concerning its frequency limits.

In this paper, we show, for the first time, that the modelization of the PBT do not require to have a continuous recourse to a 2-D numerical simulation program, and we give a definitive answer to the high frequency performances of the device. To reach these results : (i) we have worked in the buried base PBT, and (ii) we have utilized the 2-D numerical program (TITAN+JUPIN) of CNET/CNS. Evidently, the PBT is a short channel MESFET. So, we have studied the half period of the structure  $\left( L = \frac{a+d}{2} ; \text{Fig. 1} \right)$ , and we have supposed that the device is limited in its active zone :  $W_E + W_C$  ; the device bias are then applied on the limits of these zones ( $V'_{BE}$  and  $V'_{CB}$ ).

## 2. Similitude Laws for Low Collector Bias

We suppose here that in the electron velocity expression :  $\bar{V}_n = \mu_n \bar{E}$ , the mobility is constant. Besides, we adopt the classical hypothesis : (i) SCR totally depleted, (ii) at SCR boundaries,  $\frac{\partial \phi}{\partial \bar{n}} = 0$ , and (iii) into the channel  $n \approx N_D$ .

The study of Poisson equation with its boundary conditions shows that, if one takes  $\frac{d}{2}$  as the length unity, and  $\frac{qN_D d^2}{\epsilon}$  as the potential unity, the potential  $\phi(X, Y)$  depends only

on the two dimensionless parameters  $X = \frac{2W_E}{d}$ ;  $Y = \frac{2W_C}{d}$ , where  $W_E$  and  $W_C$  are the lengths of SCR around the base :

$$W_E = \left[ \frac{2\epsilon}{qN_D} (V_D - V'_{BE}) \right]^{1/2} ; W_C = \left[ \frac{2\epsilon}{qN_D} (V_D - V'_{BE} + V'_{CE}) \right]^{1/2} \quad (1)$$

We show then that the transistor current can be written as :

$$I_C = -\frac{q^2 N_D^2 \mu_n Z d^2}{4\epsilon} f\left(\frac{2W_E}{d}, \frac{2W_C}{d}\right) \quad (2)$$

To determine the function  $f(X, Y)$ , it is sufficient to plot the  $I_C(V'_{BE}, V'_{CE})$  characteristics for only one set of technological parameters  $\left(\frac{d}{2}, N_D, \mu_n\right)$ . Therefore, using the 2-D numerical program for calculating the current characteristics of only one (non particular) PBT, we can calculate analytically the characteristics of any other device.

The threshold voltage of PBT (for  $V_{CE} = 0$ ) can also be calculated :

$$I(0) = H(0)W_E ; V_{BET} = V_T \text{ for } \frac{d}{2} - I(0) = 0, \text{ so, } V_T = V_D - \frac{q}{2\epsilon H^2} N_D d^2 \quad (3)$$

The simulated characteristics give :  $H(0) \approx 0,7$ .

### 3. High Collector Bias Regime

The used model takes  $\bar{V}_n = V_s \frac{\bar{E}}{E + E_C}$  with  $V_s = 1.04 \times 10^7 \text{ cm} \cdot \text{s}^{-1}$ ;  $E_C = 1.04 \times 10^4 \text{ Vcm}^{-1}$

The current  $I_C$  can be written :

$$I_C = -qN_D Z V_m \left[ \left( \frac{d}{2} - h \right) \right] \quad (4)$$

where  $V_m$  is an average velocity ;  $V_m$  and  $h$  are, *a priori*, dependent from bias, doping ( $N_D$ ) and  $\frac{d}{2}$ . Using the 2-D program, we show that : (i)  $V_m$  and  $h$  are independent from

$\frac{d}{2}$ , (ii)  $V_m$  is independent from  $V'_{BE}$ , (iii) we can write :  $h = H(N_D, V'_{CE})W_E$ ,

$$\text{(iv) } H = 0.705 - 0.0525 V'_{CE} \quad (5)$$

so  $H$  is, in a first approximation, independent from  $N_D$ ,

(v) satisfactory analytical expression for  $V_m$  is :

$$V_m = \frac{V'_{CE}}{V'_{CE} + E_C (W_{E_0} + W_{C_0})} \quad (6)$$

$W_{E_0}$  and  $W_{C_0}$  being the values for  $V'_{BE} = 0$ .

We establish so a universal expression for  $I_C$  :

$$I_C = -qN_D Z V_m \left[ \frac{d}{2} - HW_E \right] \quad (7)$$

with  $V_m$  and  $H$  given by (6) and (5).

These analytical expressions fit very satisfactorily the 2-D simulations (Fig. 2 for example, where the dots correspond to the analytically calculated current). The 2-D simulations allow us to find also an analytical expression for the total charge in the SCR :

$$Q_{SC} = qN_D ZS = qN_D Z(W_E + W_C) \left[ \frac{a}{2} + \alpha_0 \frac{W_E(W_E + W_C)}{3W_E + W_C} \right] \quad (8)$$

we find  $\alpha_0 = 0.77$ .

#### 4. Small Signal Parameters; Frequency Limits

Using the analytical expressions of current (7) and charge (8), we can calculate : the conductance  $g_D$ , the transconductance  $g_m$  and the interelectrode capacitances  $C_{BE}$  and  $C_{BC}$ . The unity current gain (transition) frequency is then calculated :

$$f_T = \frac{g_m}{2\pi(C_{BE}(C_{BE} + 2C_{BC}))^{1/2}} \quad (9)$$

$$g_m = Z \frac{\epsilon}{W_E} V_m H$$

$$C_{BE} = Z \frac{\epsilon}{W_E} \left[ \left( \frac{a}{2} \right) + \alpha_0 W_C \frac{(1+\gamma)}{(1+3\gamma)^2} (6\gamma^2 + 3\gamma + 1) \right] \quad )$$

$$C_{BC} = Z \frac{\epsilon}{W_E} \left[ \left( \frac{a}{2} \right) \gamma + \alpha_0 W_C \frac{(1+\gamma)}{(1+3\gamma)^2} \gamma^2 (5\gamma + 1) \right] \quad ) \quad (10)$$

$$\gamma = \frac{W_E}{W_C} = \left[ \frac{V_D - V'_{BE}}{V_D - V'_{BE} + V'_{CE}} \right]^{1/2} \quad )$$

#### 5. Conclusion and Remarks

The  $f_T$ , corresponding to the Fig. 2 parameters, is not higher than 30 GHz (Fig. 3). This result is confirmed by all the published experimental works [2,3,4,5,6,7] ; the PBT on GaAs has the same limits ( $V_s$  is nearly the same for Si and GaAs) ; the etched groove PBT can be slightly better ( $C_{BE}$  is lower) ; the maximum frequency oscillations, according to our estimations, must be higher than 100 GHz ; so, the PBT, as it can deliver an important power, can be an interesting device for high frequency power amplification [8].

#### References

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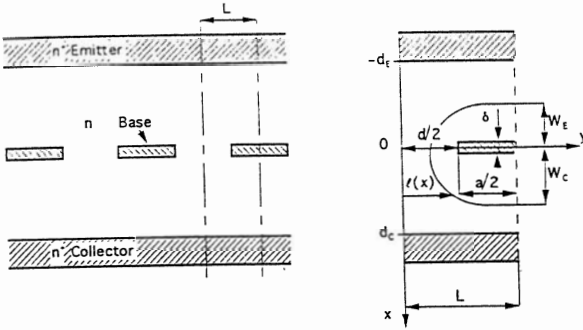


Fig. 1

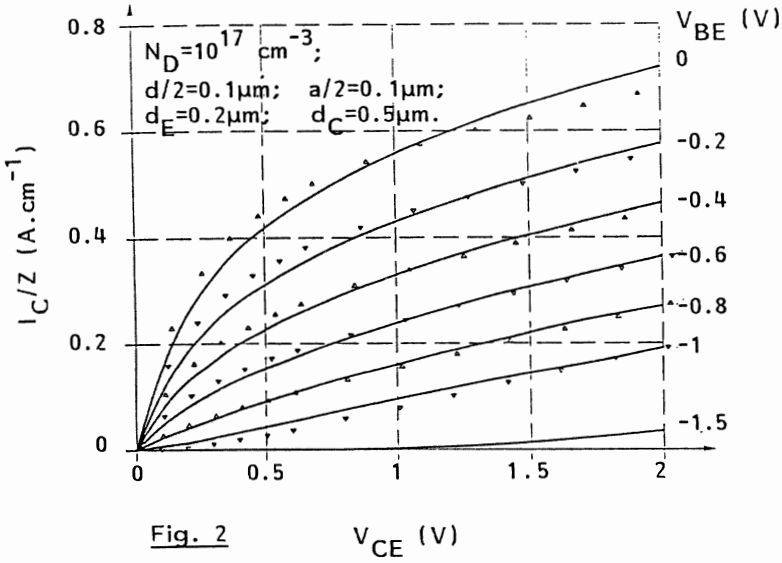


Fig. 2

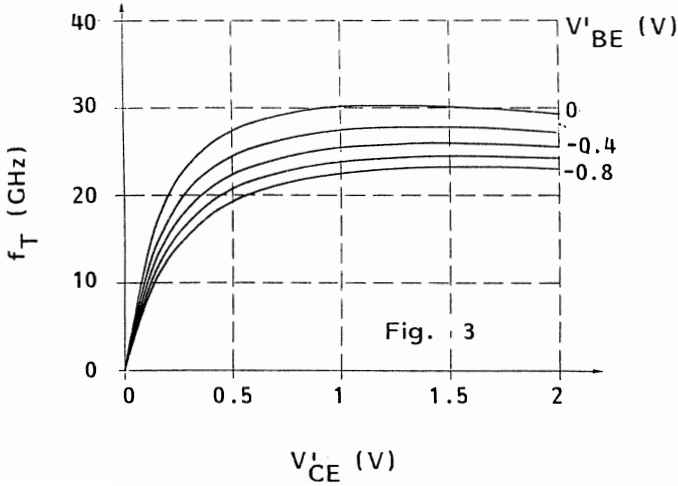


Fig. 3