# 3-D Modeling of Fringing Gate Capacitance in Gate-all-around Cylindrical Silicon Nanowire MOSFETs

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Abstract—In this paper, an analytical model for fringing gate capacitance in gate-all-around cylindrical silicon nanowire MOSFETs (SNWTs) is proposed. The fringing gate capacitances of the SNWT are divided into three parts: sidewall capacitance  $C_{gsd}$ ; parallel capacitance  $C_{gsd}$ ; perpendicular capacitance  $C_{gex}$ . Each capacitance is calculated using the following methods: conformal mapping, integral and non-dimensionalization. The proposed model is verified with a three-dimensional field solver, Raphael. Based on the proposed model, the fringing capacitance can be easily predicted in the vertically and horizontally stacked multi-wire SNWTs.

# I. INTRODUCTION

As the traditional planar MOSFET continues to scale down [1], the control of short-channel effects becomes increasingly difficult in planar-bulk architecture. Recently, the gate-allaround silicon nanowire MOSFET (SNWT) is attractive due to the following: its high immunity to short-channel effects, drain induced barrier lowering, high gate controllability, and reduction of leakage current [2]. The gate capacitance of a transistor is an important factor in determining the circuit performance with respect to the intrinsic delay in digital circuits and the transit frequency of analog circuits. Outer fringing capacitances become significant portion of the total gate capacitance, since the device gate length is reduced to below 90 nm [3]. Former fringing capacitance models in planar structure cannot predict the capacitance of 3-D structure like SNWT. Jibin et al. [4] derives parasitic gate capacitance models using equivalent transformation and inversion of Schwarz-Christoffel mapping. In this paper, we derive analytic outer fringing capacitance models using conformal mapping [5], [6], integral method [7], and non-dimensionalization technique [8] for the SNWT structures. Using non-dimensionalization technique with the dimensionless parameter created from the product of physical variables, we reduce the number of fitting parameters. The accuracy of the developed model is verified with 3-D field solver called Raphael [9].

#### II. CAPACITANCE MODELING

# A. Fringing Capacitance component

A three-dimensional structure of a single-wire SNWT structure is shown in Fig. 1(a). An SNWT structure with source/drain extension regions between an undoped channel and a heavily doped source/drain is considered. Its cross sectional view of the top and side is shown in Fig. 1(b) and



Fig. 1. (a) Three-dimensional schematic of a SNWT structure. (b) Gate and Source/Drain side view of SNWTs.  $H_g$  represents the height of the gate and  $W_g$  represents the width of the gate along the horizontal direction.



Fig. 2. Two-dimensional sectional view of SNWTs. The outer fringing capacitance ( $C_{of}$ ) is divided into three part, i.e.,  $C_{side}$ ,  $C_{gsd}$ , and  $C_{gex}$ . The basic assumption is that source and drain side are equal. We can find the  $C_{of}$  by considering one side.

Fig. 2. The fin radius is defined as r.  $t_{ox}$  is the thickness of the gate oxide surrounding the fin.  $H_g$  represents the vertical gate height, and  $W_g$  represents the width of the gate along the horizontal direction.  $H_{sd}$  and  $W_{sd}$  are source/drain height and width in the gate direction. Length of source/drain, extension and substrate region is  $L_{sd}$ ,  $L_{ext}$ , and  $L_g$ . For multi-wire SNWTs, most capacitances can be acquired by the superposition of a single-wire SNWT. Therefore, in this paper, we will mainly study the capacitance modeling of a single-wire SNWT. The total outer fringing capacitance is the sum of  $C_{side}$ ,  $C_{gsd}$ , and  $C_{gex}$  (1).

$$C_{of} = C_{side} + C_{gsd} + C_{gex} \tag{1}$$

 $C_{\text{side}}$  is the sidewall capacitance between the gate and the



Fig. 3. (a) Electric field lines between the sidewall of the gate and the S/D extension region. Dashed lines present  $C_{gex}$ . (b) The gate sidewall is empirically divided into four parts (S<sub>1</sub>-S<sub>4</sub>). To use conformal mapping method, nanowire fin can be approximated as a rectangular structure.



Fig. 4. Schematic of the  $C_{gex}$  calculation method.  $C_{gex,top}$  contains  $S_1$  and  $S_2$  parts.  $C_{gex,side}$  contain  $S_3$  and  $S_4$  parts.

source/drain region;  $C_{gsd}$  is the parallel capacitance between the gate and the source/drain region;  $C_{gex}$  is the rectangular capacitance between the gate and the extension region.

#### B. Analytical modeling using conformal mapping

In order to simply define the analytical model of the complex electrostatic system between the gate, source/drain extension region, and source/drain region, it is assumed that the extension region, source/drain, and the sidewalls of source/drain are uncorrelated in deriving the total outer fringing capacitance. Thus, we can divide total outer fringing capacitance into  $C_{side}$ ,  $C_{gsd}$ , and  $C_{gex}$ , as mentioned. The sidewall capacitance  $C_{side}$  is formed by the top, bottom, and two-side surface along the direction parallel to channel region, so that the  $C_{side}$  is derived by multiplying circumference of the gate and  $C_{side}$  per unit distance (2).

$$C_{side} = \frac{\epsilon_{di}}{2\pi} \ln(1 + \frac{2L}{L_{ext}}) \times 4(W_g + H_g + 2r + 2t_{ox}) \quad (2)$$

 $C_{side}$  per unit distance which consist of two coplanar plates can be calculated using the integral method in two equal plates (L=L<sub>sd</sub>=L<sub>g</sub>). The system of two unequal plates can be transformed into the two equal coplanar plates by applying the empirical equation L over L<sub>ext</sub>. The empirical equation can be defined by the non-dimensionalization method (3).

$$\frac{L}{L_{ext}} = 31.02 \left[ \frac{\sqrt{(L_{ext} + L_g)(L_{ext} + L_{sd})L_g L_{sd}}}{(L_{ext} + L_g + L_{sd})L_{ext}} \right]^{1.4}$$
(3)

The parallel capacitance,  $C_{gsd}$ , represents the electric coupling between adjacent sidewalls of the gate and source-drain regions. We can model  $C_{gsd}$  as two parallel plates with effective



Fig. 5. For multiwire SNWTs,  $W_g$  and  $H_g$  are the half of the thickness between adjacent wires. Number of stacked wire each side is N and M.

area and distance (4).

$$C_{gsd} = \epsilon_{di} \frac{4(H_g + t_{ox} + r)(W_g + t_{ox} + r) - \pi(r + t_{ox})^2}{L_{ext}}$$
(4)

The analytical equation for  $C_{gex}$  is derived by transforming the electric field into equivalent quasi-confocal elliptical system, as shown in Fig. 3(a). Fig. 3(b) shows the transformation of fin and oxide. We can approximate the circular fin into quadrangle fin, and empirically divide into four parts (S<sub>1</sub>-S<sub>4</sub>) to use conformal mapping.  $C_{gex}$  is formed by  $C_{gex.top}$  which contains S<sub>1</sub> and S<sub>2</sub> and  $C_{gex.side}$  which contains S<sub>3</sub> and S<sub>4</sub>, as shown in Fig. 4 and in (5).

$$C_{gex} = 2(C_{gex.top} + C_{gex.side}) \tag{5}$$

To model the analytical equation  $C_{gex}$  precisely, it can be assumed that  $C_{gex.top}$  and  $C_{gex.side}$  are not related to each other.  $C_{gex.top}$  and  $C_{gex.side}$  are calculated by conformal mapping and empirical fitting parameter,  $\eta$  and  $\delta$  (6)-(9).  $C_{gex.top}$  and  $C_{gex.side}$ per unit distance can be obtained by conformal mapping method between two perpendicular planes in ideal case.  $H_g$ ,  $W_g$ ,  $t_{ox}$ , and  $L_{ext}$  are part of the two ellipses of the same focus without any electrical interference. The empirical parameter  $\eta$  denotes the compensation of the focus offset from the difference from the ideal ellipse. In order to expend the  $C_{gex.top}$ and  $C_{gex.side}$  which contain the trapezoidal plane as shown in Fig. 4 from  $C_{gex.top}$  and  $C_{gex.side}$  per unit distance, we can define the equation  $\delta$  that consists of parameters related thickness:  $W_g$ ,  $H_g$ , r, and  $t_{ox}$ .

$$C_{gex.[top,side]} = \frac{2\epsilon_{ox}}{\pi} \delta_{[top,side]} \times \ln\left[\frac{t_{ox} + \eta_{[top,side]}[H_g, W_g] + \tau_{[top,side]}}{t_{ox}}\right]$$
(6)

where

$$\delta_{[top,side]} = \frac{[W_g, H_g]}{2\pi} + 2r + \frac{2t_{ox}}{\pi}$$
(7)



Fig. 6. Comparison between the outer fringing capacitandce model (lines) and the 3-D numerical simulation results (symbols) as a function of various device parameters. (a)  $C_{of}$  verification at  $L_{ext} = 20$  nm and 50 nm. (b) and (c)  $C_{of}$  as a function of r and  $L_{ext}$  at  $H_g = 40$  nm, 70 nm, and 100 nm.



Fig. 7. Comparison with simulation results and a reference model (dash).  $C_{of}$  as a function of  $t_{ox}$ ,  $H_g$ , and  $L_{ext}$ .  $H_{sd}$  and  $W_{sd}$  are assumed to be equal to  $H_g$  and  $W_g$  in fig. 5(a)-(c).

$$\tau_{[top,side]} = \sqrt{(\eta_{[top,side]}[H_g, W_g])^2 + 2\eta_{[top,side]}[H_g, W_g]t_{ox}}$$
(8)

$$\eta_{[top,side]} = 3\pi \exp\left[\frac{L_{ext} - \sqrt{[H_g, W_g]^2 + 2[H_g, W_g]t_{ox}}}{L_{ext}}\right]$$
(9)

Based on (1)-(9), the expression of outer fringe capacitance can be derived in multi-wire SNWTs, as shown in Fig. 5. The number of the channels connected in parallel along the vertical and horizontal direction is defined as N and M. H<sub>g</sub> and W<sub>g</sub> represent the half of the gate electrode thickness in between adjacent wires. The total outer fringing capacitance in multiwire SNWTs C<sub>of.m</sub> is the sum of the rectangular capacitance, the parallel capacitance, and the sidewall capacitance as same component as a single-wire SNWT (10). The rectangular and parallel capacitances are derived by the multiplying C<sub>gex</sub> and C<sub>gsd</sub> by the number of wires. The sidewall capacitance represents the multiplying unit length of C<sub>side</sub> by the circumference of the gate in multi-wire SNWTs. In case of M and N are 1, C<sub>of.m</sub> is same as total outer fringing capacitance in a singlewire SNWT.

$$C_{of.m} = (C_{gex} + C_{gsd}) \times MN + C_{side} \times \frac{M(H_g + r + t_{ox}) + N(W_g + r + t_{ox})}{W_g + H_g + 2r + 2t_{ox}}$$
(10)

In addition,  $C_{of.m}$  over M and N is the outer fringing capacitance per unit number of channel in multi-wire SNWT (11). The rectangular and parallel capacitance per wire is the same as  $C_{gex}$  and  $C_{gsd}$ . On the other hand, since the fraction multiplied by  $C_{side}$  has a value less than 1, the sidewall capacitance per wire is smaller than  $C_{side}$ . Thus, multi-wire architecture should be preferred than the single-wire architecture from the perspective of reducing the gate fringing capacitance.

$$C_{of.m}/MN = C_{gex} + C_{gsd} + C_{side} \times \frac{W_g/M + H_g/N + r(\frac{1}{M} + \frac{1}{N}) + t_{ox}(\frac{1}{M} + \frac{1}{N})}{W_g + H_g + 2r + 2t_{ox}}$$
(11)

# **III. SIMULATION RESULTS**

The accuracy of this outer fringing capacitance model is verified over a wide range of geometrical parameters such as  $H_g$ , r,  $L_{ext}$ , and  $t_{ox}$  by 3-D numerical simulations. Excellent agreement is achieved with the proposed model, as shown in Fig. 6. Fig. 7 also shows that the proposed model has better accuracy than the model in the reference paper by Jibin et al. compared to 3-D simulation results. Fig. 8 shows the proposed model validation for multi-wire SNWTs. There is a good agreement between the modeled results and Raphael 3D simulated results for M and N variations. For larger N, the total gate capacitance increases. However, the total gate capacitance per width decresaes due to  $C_{side}$  differences, as shown in Fig.



Fig. 8. Comparison between the outer fringing capacitandce model (lines) and the 3-D numerical simulation results (symbols) as a number of stacked nanowire.



Fig. 9. Comparison between the outer fringing capacitandce model (lines) and the 3-D numerical simulation results (symbols) per wire as a number of stacked nanowire.

9. In addition, Fig. 10 shows the change of  $C_{of.m}$  as a function of total gate width over a radius for 3 by 3 multi-wire SNWTs. For radii of 3, 4 and 5, excellent accuracy of  $C_{of.m}$  is obtained, and the contribution of fringing capacitance can be reduced by reducing the radius of a single wire when wire pitch are kept constant.

# IV. CONCLUSION

In this paper, a comprehensive model for parasitic outer fringing gate capacitance is proposed for gate-all-around cylindrical SNWTs. The proposed analytical model can be implemented as a compact model for accurate circuit simulations. In the development of fringing capacitance model, a practical SNWT structure was considered with the gate, source/drain, and extension regions. We analyze the effects of geometrical parameter variation on the fringing capacitance of SNWTs. The total 3-D fringing capacitance is decomposed into two-dimensional components each of which is derived with a conformal mapping technique, integral and non-dimensionalization method. The accuracy of the proposed model is verified with the results of three-dimensional field solver, Raphael.



Fig. 10. The outer fringing gate capacitance for 3 by 3 multi-wire SNWTs as a function of total gate width for different radii.

#### V. ACKNOWLEDGEMENT

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#### REFERENCES

- [1] The International Technology Roadmap for Semiconductors (*ITRS*), 2012.
- [2] S. D. Suk, S.-Y. Lee, S.-M. Kim, E.-J. Yoon, M.-S. Kim, M. Li, C. W. Oh, K. H. Yeo, S. H. Kim, D.-S. Shin, K.-H. Lee, H. S. Park, J. N. Han, C. J. Park, J.-B. Park, D.-W. Kim, D. Park, and B.-I. Ryu, "High performance 5 nm radius twin silicon nanowire MOSFET (TSNWFET): Fabrication on bulk Si wafer, characteristics, and reliability," *IEDM Tech. Dig.*, 2005, pp. 717720.
- [3] L. Wei, F. Boeuf, T. Skotnicki, and H.-S. Philip Wong, "Parasitic Capacitance: Analytical Models and Impact on Circuit-Level Performance," *IEEE Trans. Electron Devices*, vol. 58, no. 5, pp. 13611370, May 2011.
- [4] J. Zou, Q. Xu, J. Luo, R. Wang, R. Huang, and Y. Wang, "Predictive 3-D modeling of parasitic gate capacitance in gate-all-around cylindrical silicon nanowire MOSFETs," *IEEE Trans. Electron Devices*, vol. 58, no. 10, pp. 33793387, Oct. 2011.
- [5] A. Bansal, B. C. Paul, and K. Roy, "Modeling and optimization of fringe capacitance of nanoscale DGMOS devices," *IEEE Trans. Electron Devices*, vol. 52, no. 2, pp. 256262, Feb. 2005.
- [6] A. Bansal, B. C. Paul, and K. Roy, "An analytical fringe capacitance model for interconnects using conformal mapping," *IEEE Trans. Comput.-Aided Design Integr. Circuits Syst.*, vol. 25, no. 12, pp. 2765-2774, Dec. 2006.
- [7] M. Zahn Electromagnetic Field Theory: A Problem Solving Approach, New York: Wiley, 1979.
- [8] J. D. Anderson, *Fundamentals of Aerodynamics*, 2nd ed. New York: McGraw Hill, 1991.
- [9] TCAD, Raphael Users Guide, Synopsys.