

# Thermoelectric Power Factor of Ultra-Narrow Silicon Nanowires

N. Neophytou and H. Kosina

Institute for Microelectronics, Technical University of Vienna, TU Wien

Gußhausstraße 27-29/E360, A-1040 Wien, Austria.

e-mail: [neophytou|kosina}@iue.tuwien.ac.at](mailto:{neophytou|kosina}@iue.tuwien.ac.at)

## INTRODUCTION

The thermoelectric performance of materials is determined by the figure of merit  $ZT = \sigma S^2 / (\kappa_e + \kappa_l)$ , where  $\sigma$  is the electrical conductivity,  $S$  is the Seebeck coefficient and  $\kappa_e$  and  $\kappa_l$  are the electronic and lattice contributions to the thermal conductivity, respectively. The interrelation of these quantities has traditionally kept  $ZT$  at low values, around unity. Nanomaterials have recently attracted significant attention because at the nanoscale the length scale degree of freedom offers possibilities of independent design of  $\sigma$ ,  $S$  and  $\kappa_l$  such that high  $ZT$  values can be achieved. This was demonstrated to be the case not only for the rare-earth and/or toxic usual TE materials, but also for traditionally poor TE materials such as Si. Bulk Si has a very high  $\kappa_l = 140 \text{ W/mK}$  which results in  $ZT \sim 0.01$  at 300K. Silicon nanowires (NWs), on the other hand, have demonstrated  $ZT \sim 1$  (Fig. 1) [1, 2], which makes Si a promising and abundant TE material candidate with well established industrial scale processes.

## METHOD AND DISCUSSION

Although most of the  $ZT$  enhancement of Si NWs has resulted from the drastic reduction in  $\kappa_l$  down to  $2 \text{ W/mK}$ , it is becoming evident that benefits from  $\kappa_l$  are reaching their limits, and further TE performance improvement will result from power factor ( $\sigma S^2$ ) improvements. In this work we present a comprehensive analysis of the thermoelectric power factor in Si NWs of different carrier type (n- and p-type), different diameters, and different transport and confinement orientations (Fig. 2). We employ the atomistic  $sp^3d^5s^*$  tight-binding model and linearized Boltzmann transport theory [3]. We identify the design parameters that have the strongest influence on the power factor and identify bandstructure optimization directions. Our conclusions are of general relevance for the optimal

design of the TE power factor of low dimensional materials.

The Seebeck coefficient in NWs depends at first order on the distance of the band edges from the Fermi level ( $\eta_F$ ). At a constant carrier concentration  $\eta_F$  changes differently for different NW types as a function of diameter, mainly increasing with scaling (Fig. 3a). This increase improves the power factor as the diameter is reduced below  $D = 7 \text{ nm}$  as shown in Fig. 3b (under ballistic conditions). Additionally, the carrier velocities are a strong function of NW type and can vary differently as the diameter is reduced. In some cases the carrier velocities are diameter independent (Fig. 3c), but in other cases they increase with diameter reduction (Fig. 3d).

Such property differences can be used to optimize the thermoelectric performance of NWs. For example, although under ballistic conditions the Seebeck coefficient can offer some advantages to the power factor, when phonon and surface roughness scattering (SRS) are considered, the conductivity is severely degraded with diameter reduction (Fig. 4a), and so is  $ZT$  (Fig. 4c). On the other hand, in cases where the carrier velocity increases with confinement, such as in p-type [111] NWs, the conductivity increases (Fig. 5a), which compensates for the effect of SRS and improved  $ZT$  values can be obtained (Fig. 5c).

## CONCLUSION

Ultra-thin Si NWs offer the possibility of TE power factor optimization through bandstructure engineering techniques. The Seebeck coefficient and the electrical conductivity can be optimized using confinement and orientation to achieve enhanced TE properties.

## ACKNOWLEDGEMENT

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## REFERENCES

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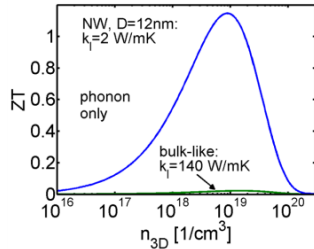


Fig. 1. The ZT figure of merit versus carrier concentration of a cylindrical NW of  $D=12\text{nm}$  calculated for  $k_l=2\text{ W/mK}$  (NW-like), and  $k_l=140\text{ W/mK}$  (bulk-like).

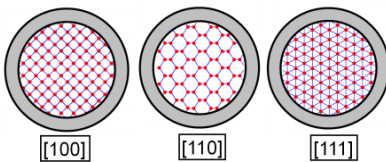


Fig. 2. Cross sections of the NWs analysed. The [100], [110] and [111] orientations. The NW surface is assumed to be hydrogen passivated.

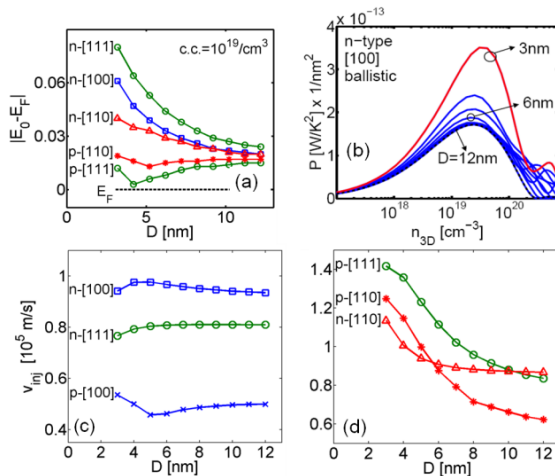


Fig. 3. (a) The shift in the band edge of n- and p-type NWs in different transport orientations vs. diameter, at carrier concentration  $10^{19}/\text{cm}^3$ . (b) The power factor (ballistic) of n-type [100] NWs with  $D=12\text{nm}$  down to  $3\text{nm}$  vs. carrier concentration. (c-d) The carrier injection velocities vs. diameter of n- and p-type NWs of different transport orientations.

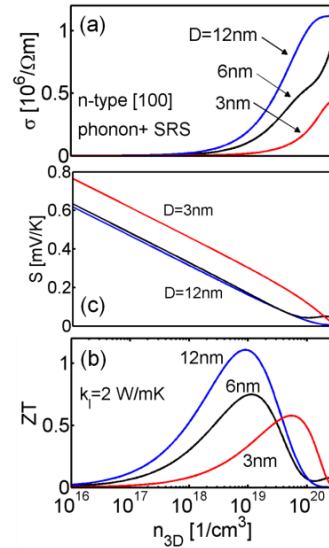


Fig. 4. Thermoelectric coefficients versus carrier concentration for n-type [100] NWs of  $D=12\text{nm}$  (blue),  $6\text{nm}$  (black) and  $3\text{nm}$  (red), at  $300\text{K}$ . Phonon scattering plus SRS are included. (a) The electrical conductivity. (b) The Seebeck coefficient. (c) The ZT figure of merit ( $k_l=2\text{ W/mK}$  is assumed for all cases).

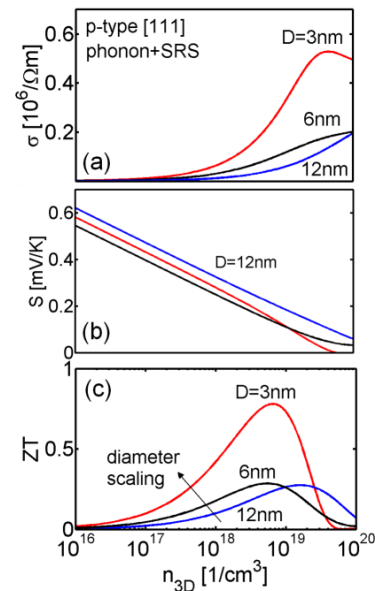


Fig. 5. Thermoelectric coefficients versus carrier concentration for p-type [111] NWs of  $D=12\text{nm}$  (blue),  $6\text{nm}$  (black) and  $3\text{nm}$  (red), at  $300\text{K}$ . Phonon scattering plus SRS are included. (a) The electrical conductivity. (b) The Seebeck coefficient. (c) The ZT figure of merit ( $k_l=2\text{ W/mK}$  is assumed for all cases).